

Polymer physics in nanoscale cutting

Opportunities for improved control in nano-manufacturing?

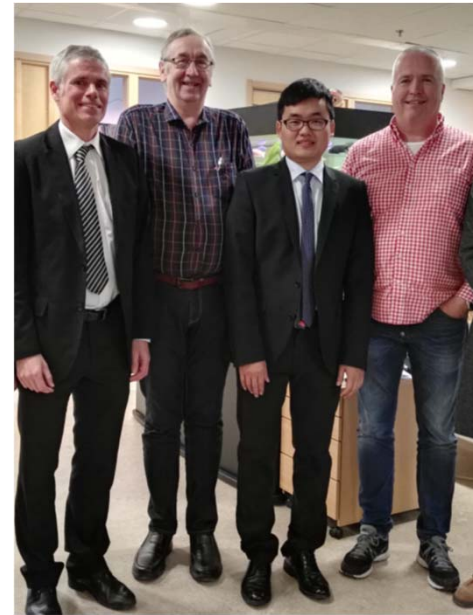
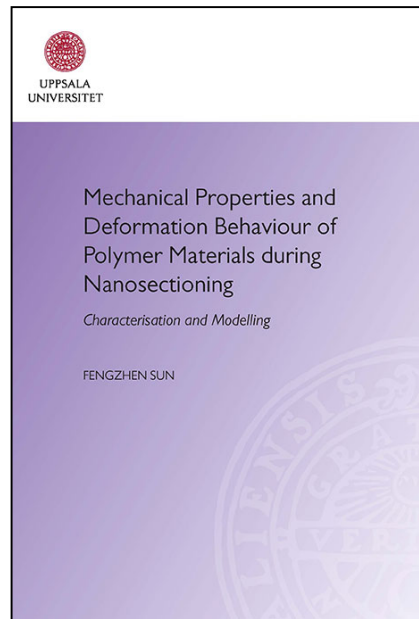
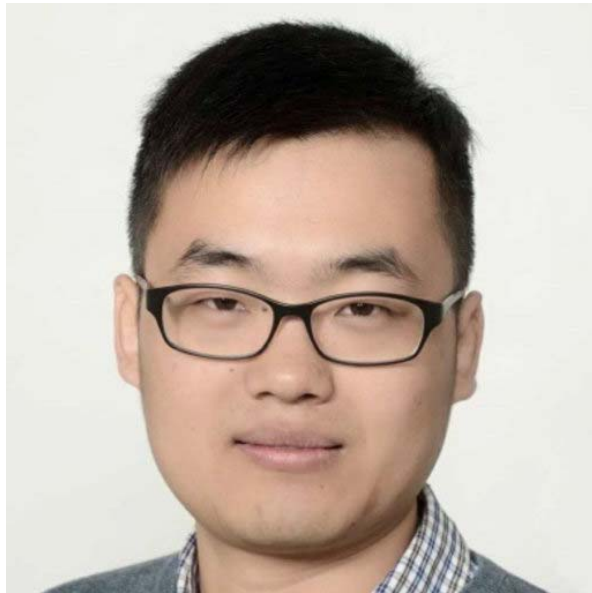


Kristofer Gamstedt, Ångström Laboratory, Uppsala University

Fengzhen Sun, presently Imperial College London

Henrik Lindberg and Mats Ericson, previously Luleå University of Technology

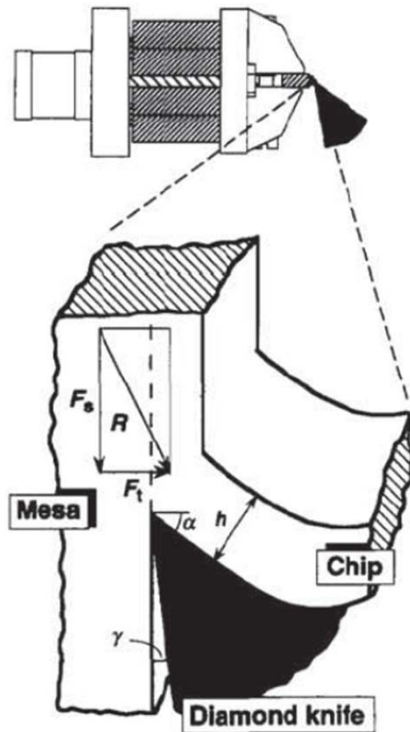
Work mainly carried out by Dr. Fengzhen Sun
PhD Uppsala University, 2017



Mats Ericson



Henrik Lindberg



Ericson, M.L. and Lindberg, H., "Design and potential of instrumented ultramicrotomy", *Polymer*, **38** (1997), 4485

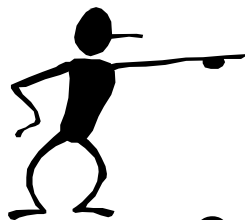
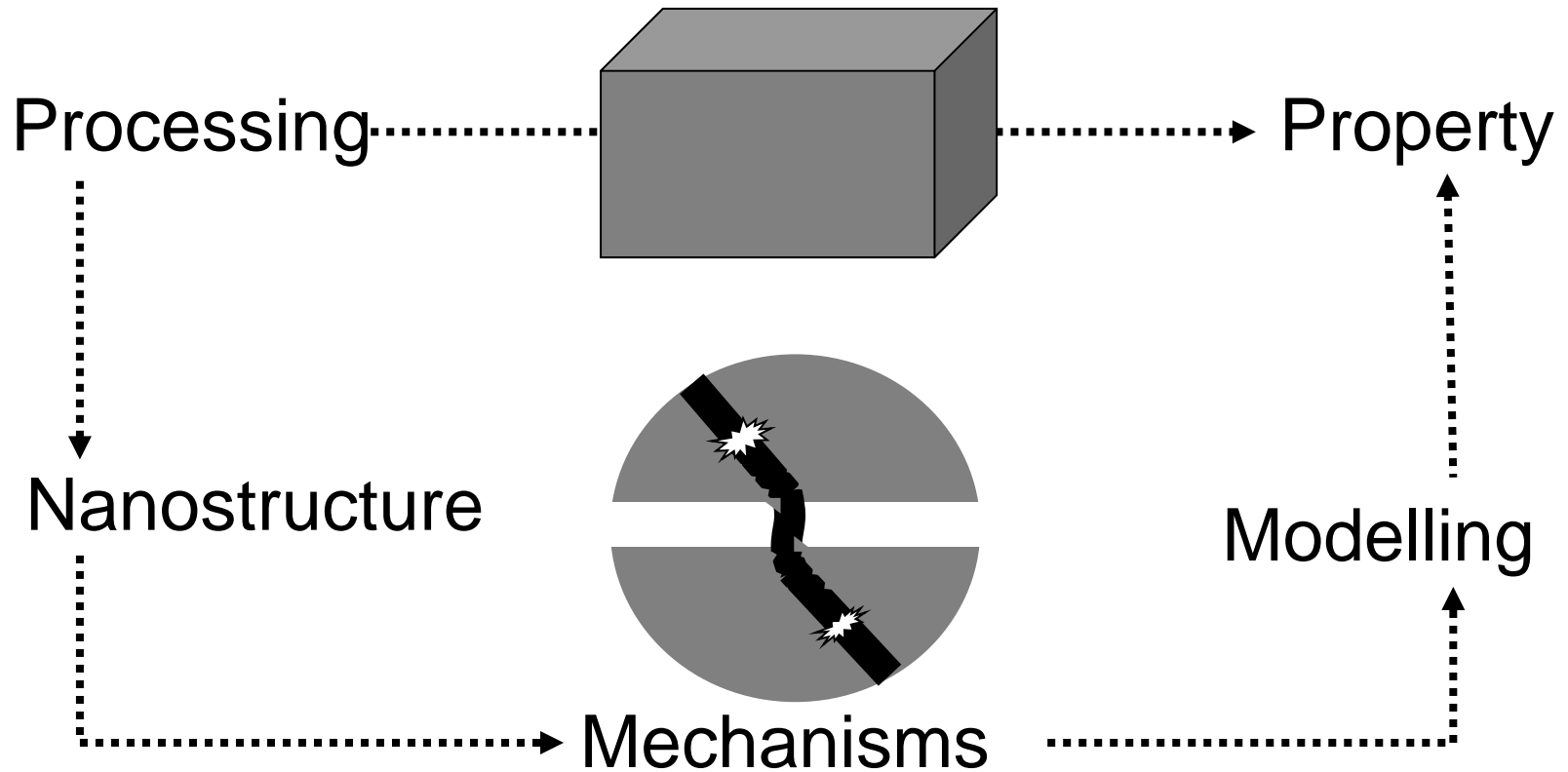
Uppsala University



Full university, founded in 1477

Physics, chemistry and engineering in the Ångström Laboratory

Background in material mechanics



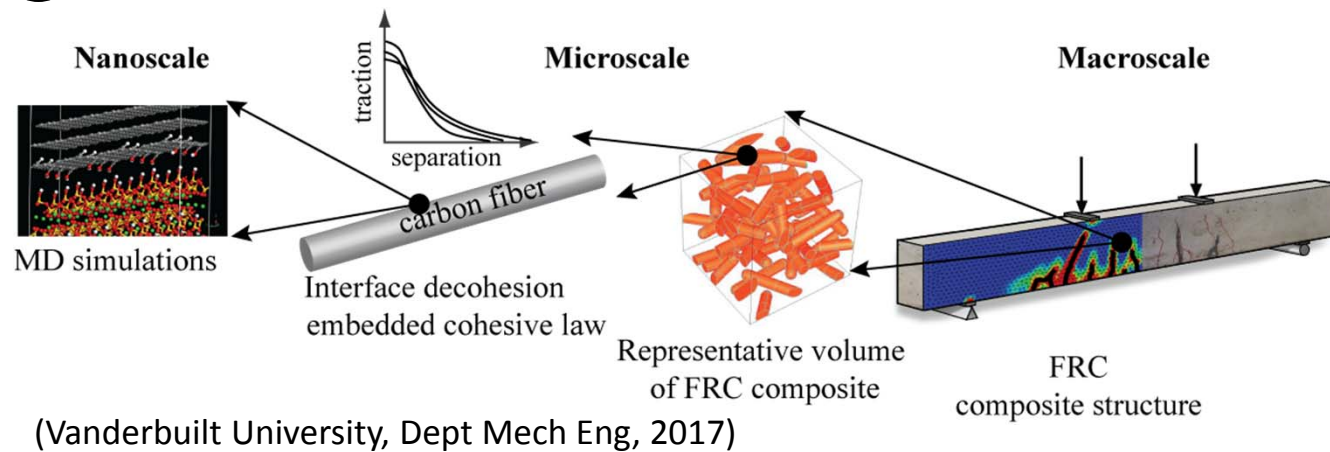
Vision:

Experiments and modelling to develop predictive tools for optimized materials design

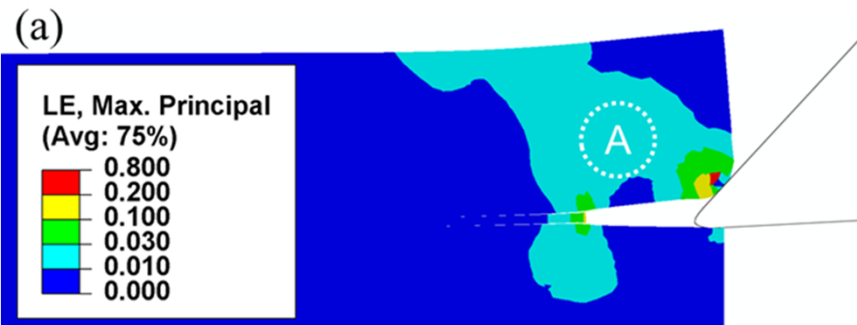
Composites, wood, paper, board, polymers, asphalt, implants...

Experimentally characterized constitutive models on nanoscale ...

① ... to predict and design nanocomposites etc.



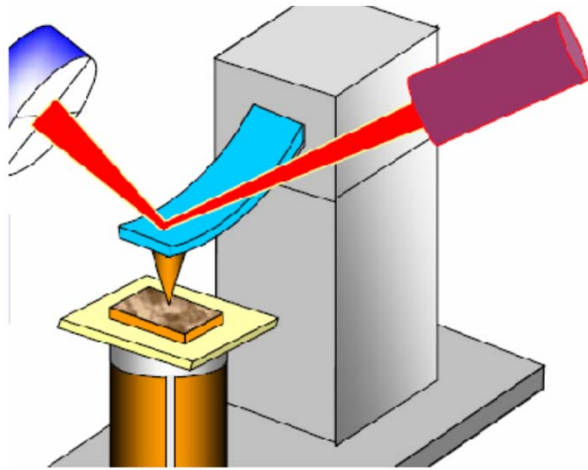
② ... to predict and control in nanomanufacturing



Cross-disciplinary fertilization:

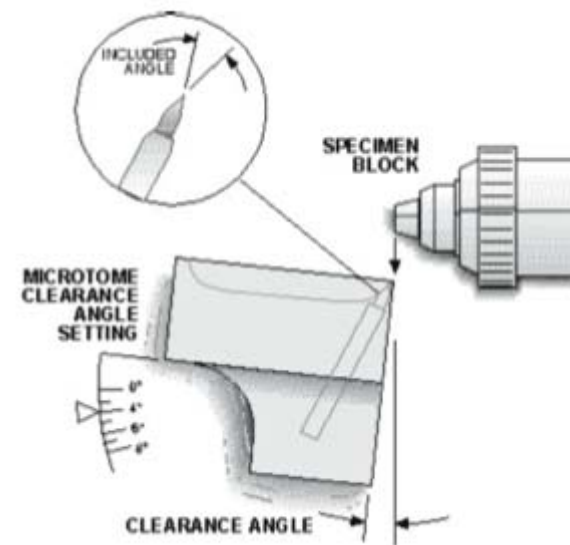
Methods developed for other applications also useful in nanomanufacturing

AFM



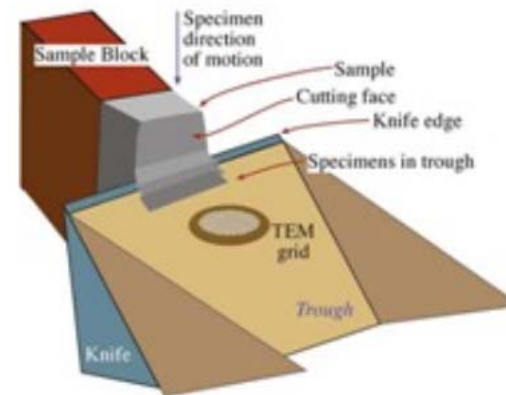
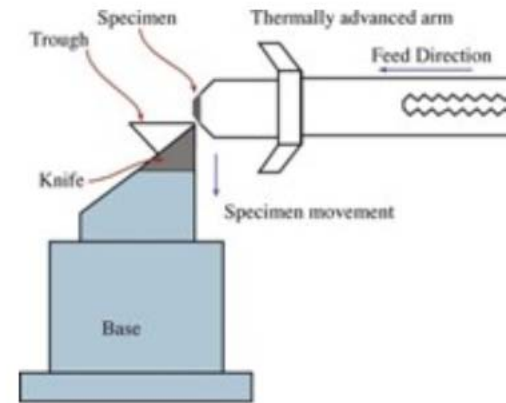
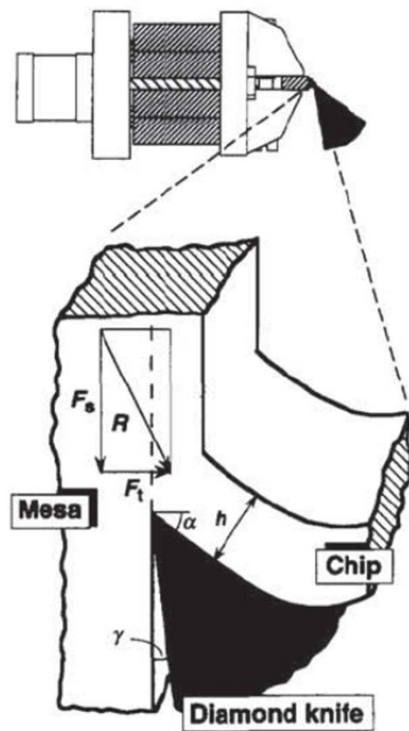
E.g. Yongda Yan (HIT), Emmanuel Brousseau (Cardiff) @ this conf.

Ultramicrotomy



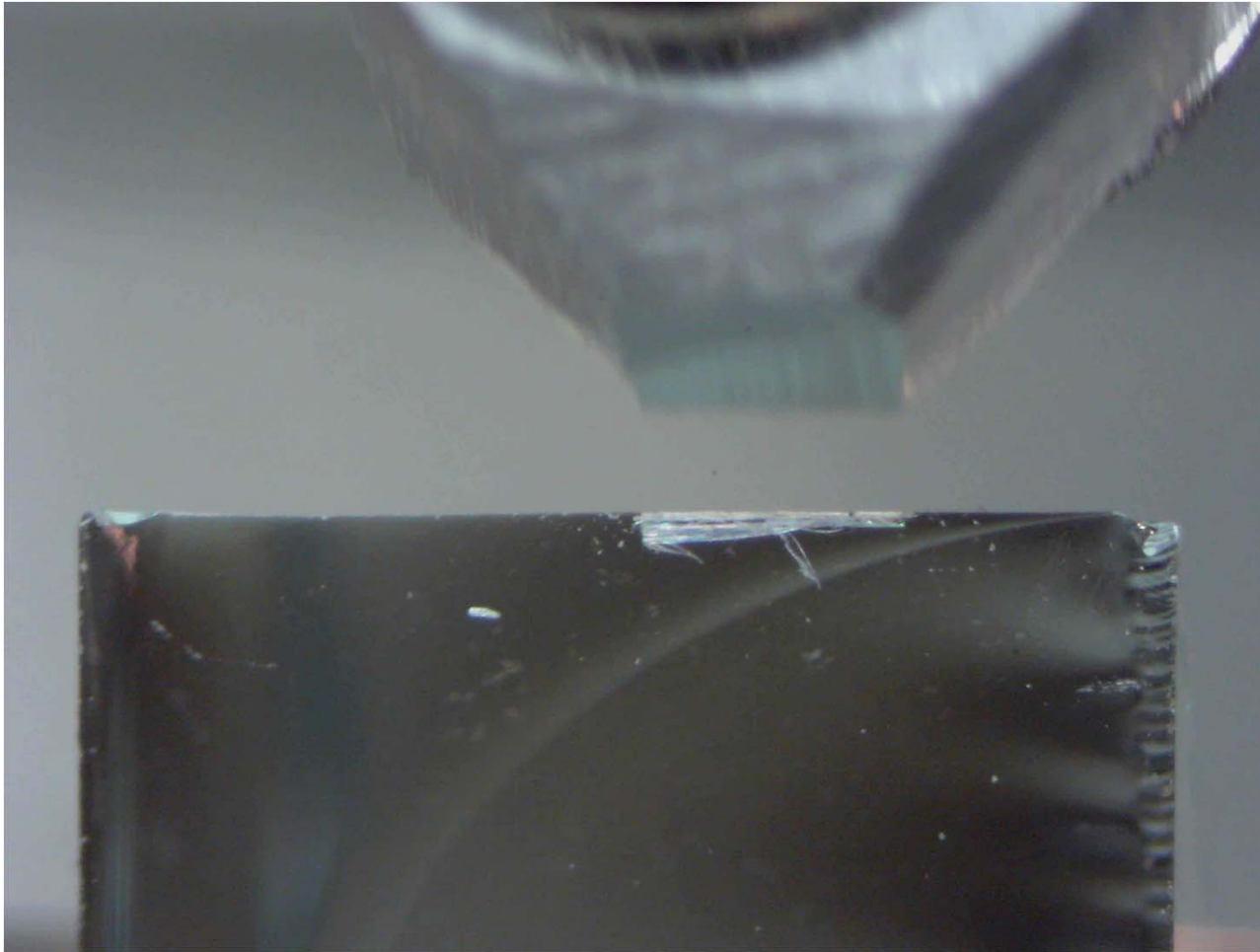
Ericson and Lindberg, 1997

Ultramicrotomy used for preparation of TEM samples

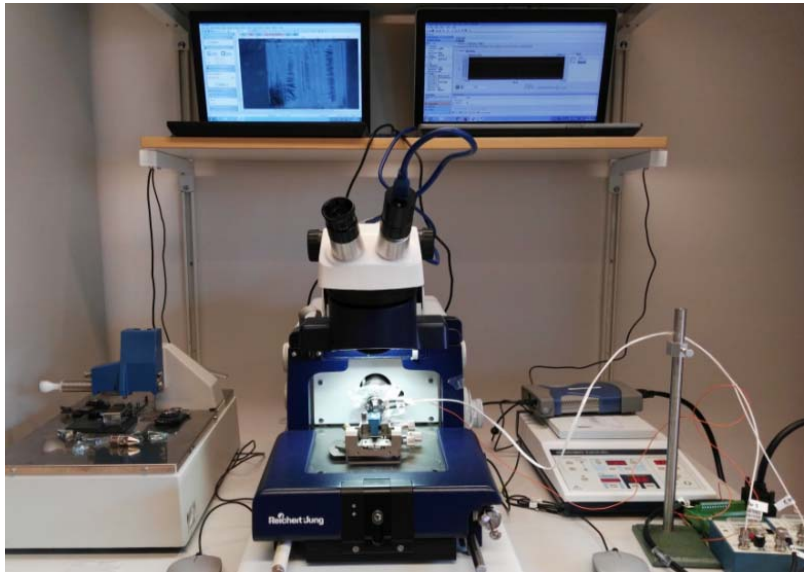


Chips with a thickness of down to ~ 30 nm

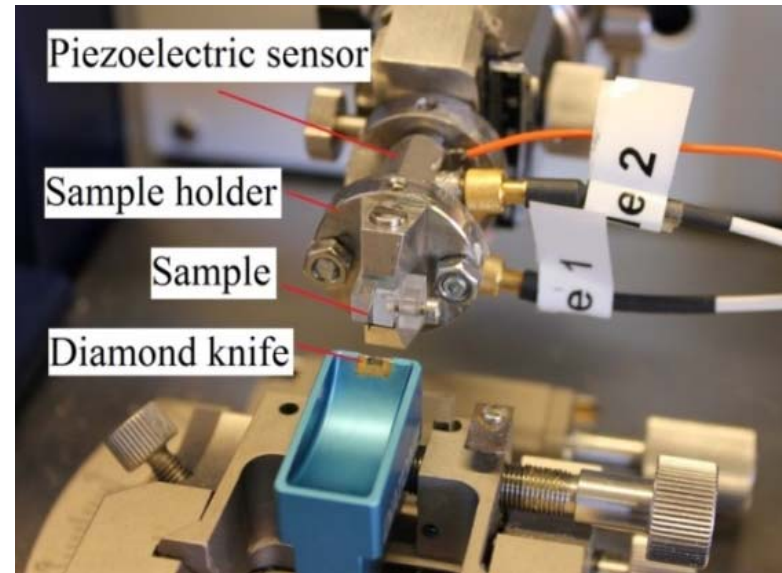
Sequential cutting of ultrathin chips in the ultramicrotome



Instrumented ultramicrotome

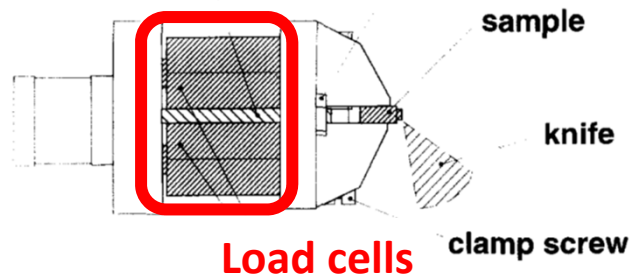


Sample holder



(Ericsson & Lindberg, 1997)

Sectioning thickness: 30-200 nm
Sectioning speed: 0.25-20 mm/s
Force sensor resolution: < 1 mN
Diamond knife: edge radius ~7 nm



Cutting force F_c



Transverse force F_t



Model material: Poly(methyl methacrylate), PMMA, acrylic glass or Plexiglas, a transparent amorphous glassy thermoplastic

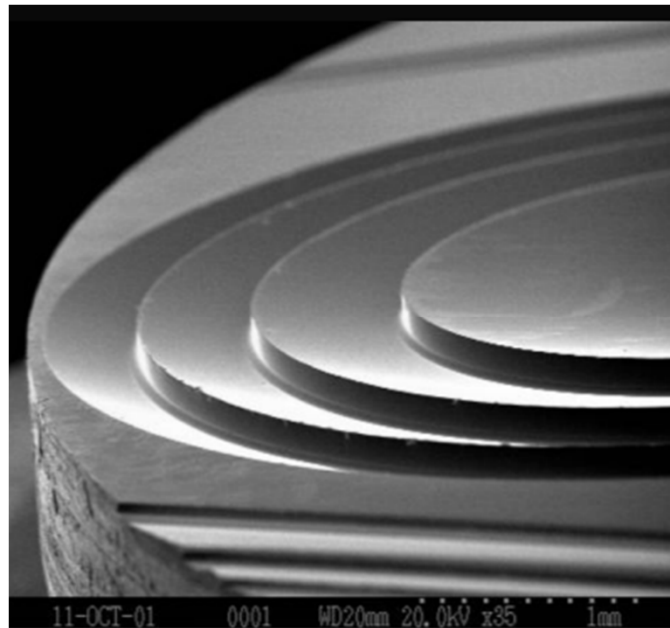




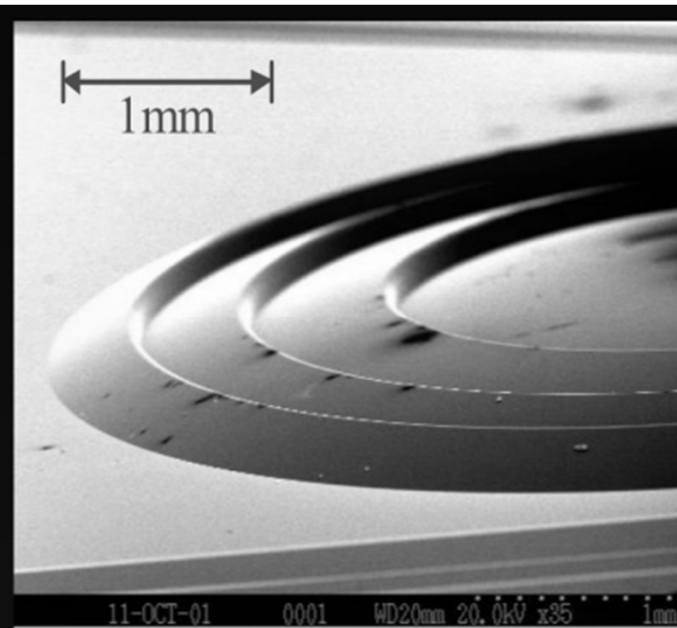
PMMA

Increasing demands on micro/nano manufacturing
(miniaturisation in optics, electronics)

Diamond machined mould



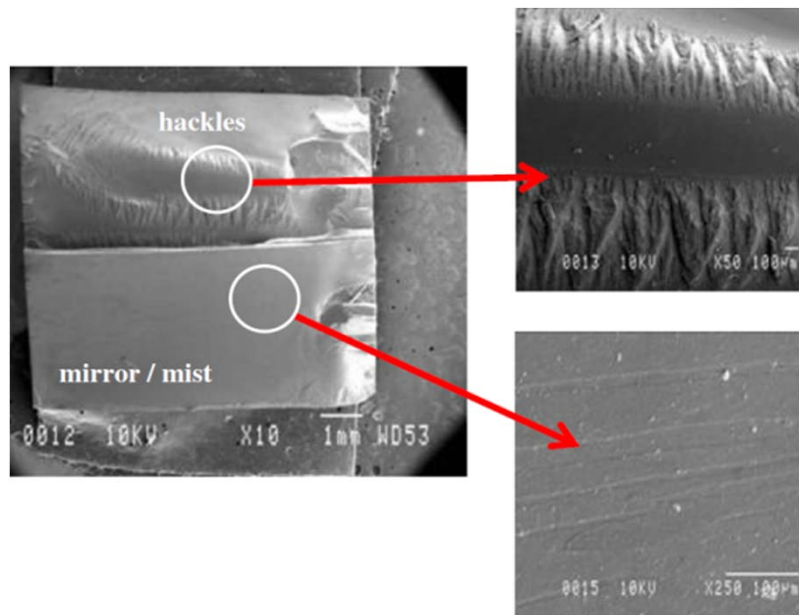
Moulded PMMA optic



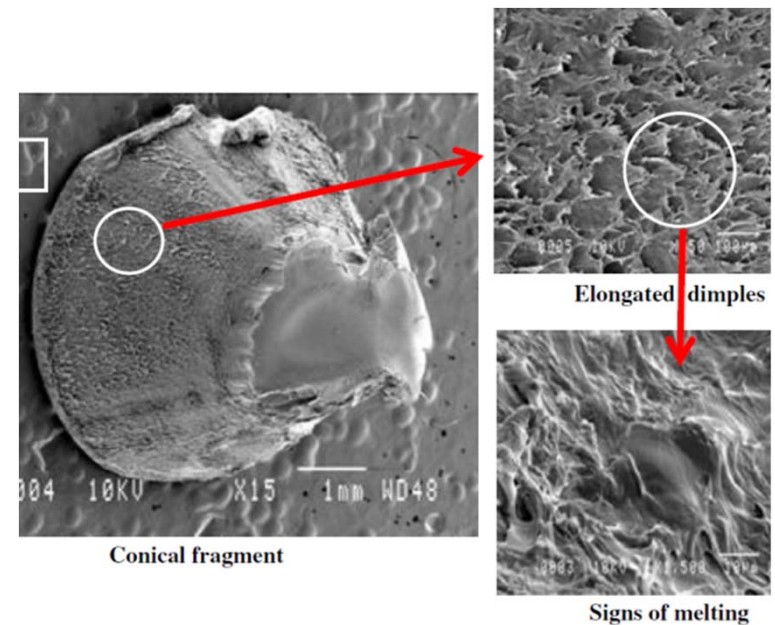
(Gill & Dow)

PMMA can show a complex deformation and fracture behaviour

Brittle failure of PMMA



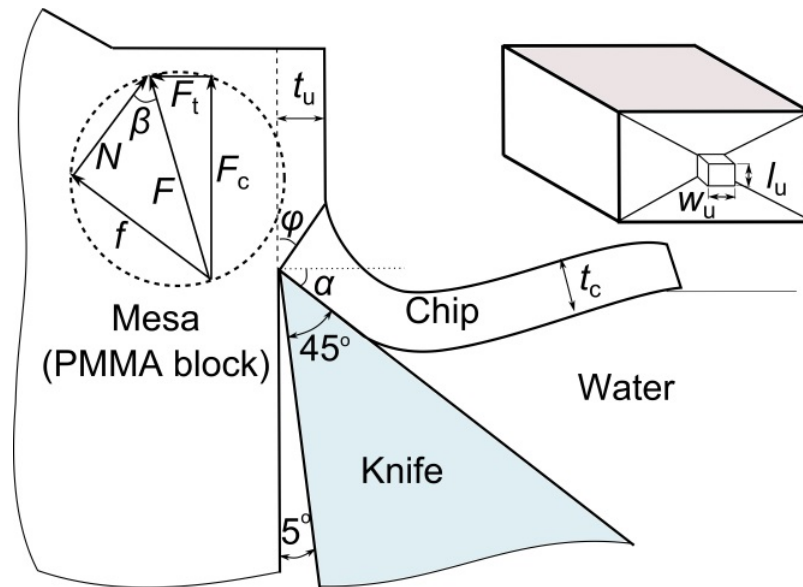
Ductile failure of PMMA



(Rittel & Brill, 2008)

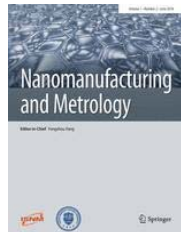
Instrumented ultramicrotomy:

Well-controlled cutting of PMMA on the nanoscale



Why?

- Measuring fracture toughness
- Investigate deformation and fracture mechanisms
- Propose predictive model
- Optimise processing conditions



Review on nanocutting: Fang & Xu, *Nanomanufacturing and Metrology* **1** (2018), 4

Fracture toughness & Yield stress

Energy balance (*Atkins, 2003*)

external work =

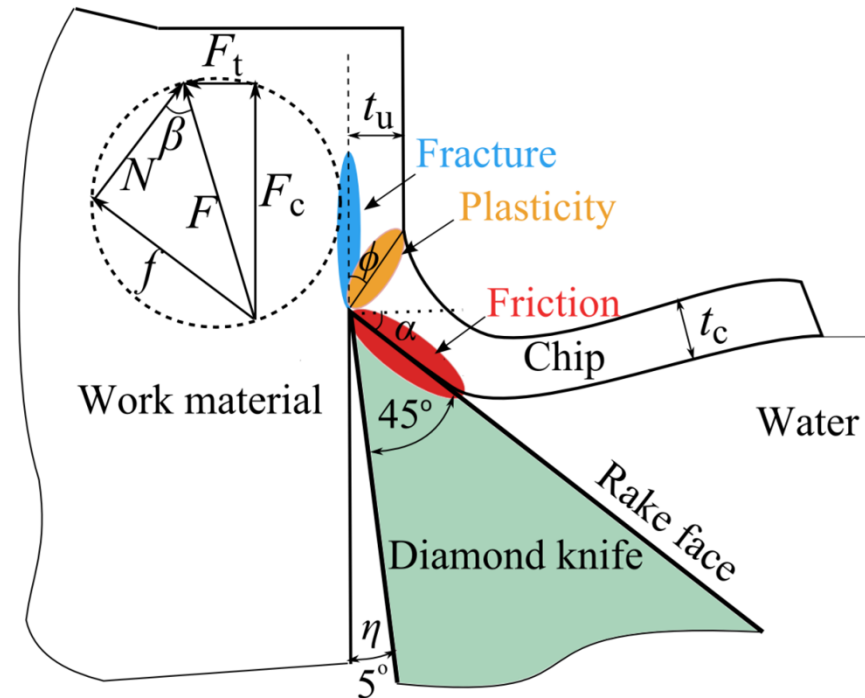
plasticity + friction + fracture

shear yield stress
MPa

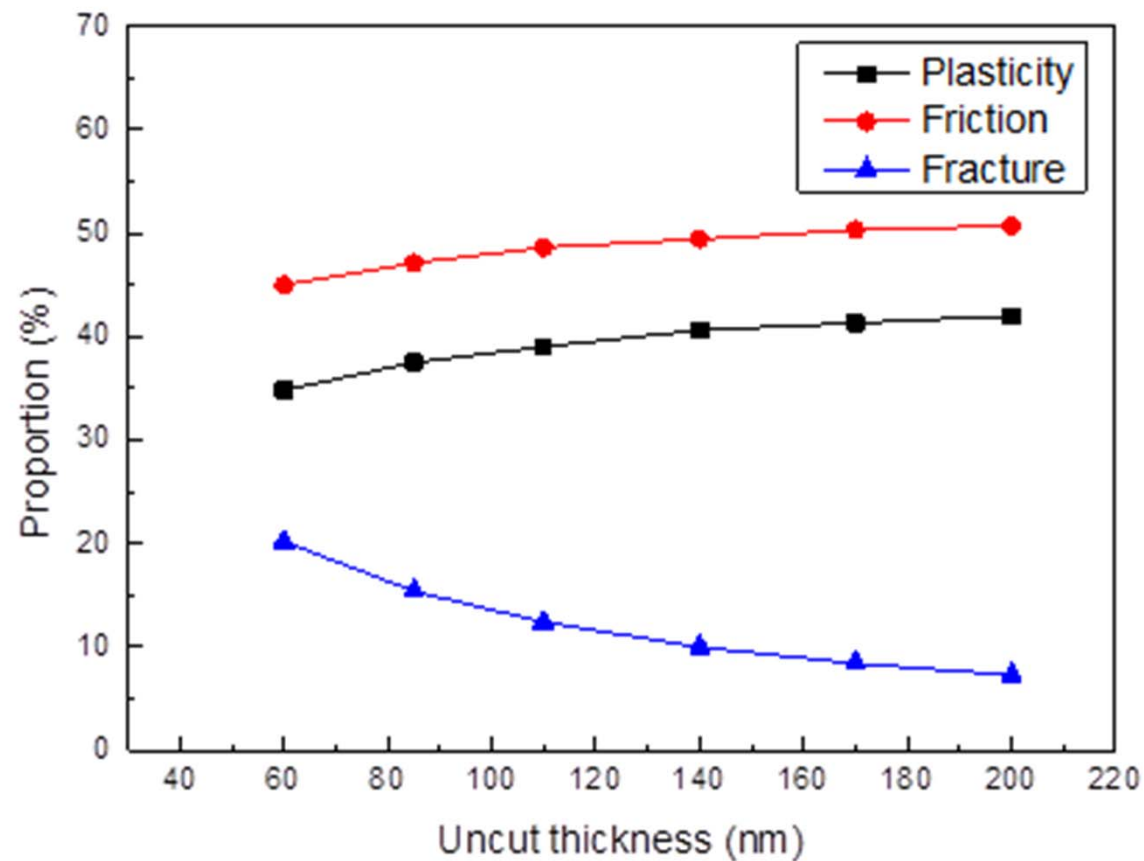
$$F_c v_0 = (\tau_y \gamma)(t_u w v_0) + [F_c \sec(\beta - \alpha) \sin \beta] \frac{v_0 \sin \phi}{\cos(\phi - \alpha)} + R w v_0$$

fracture energy
J/m²

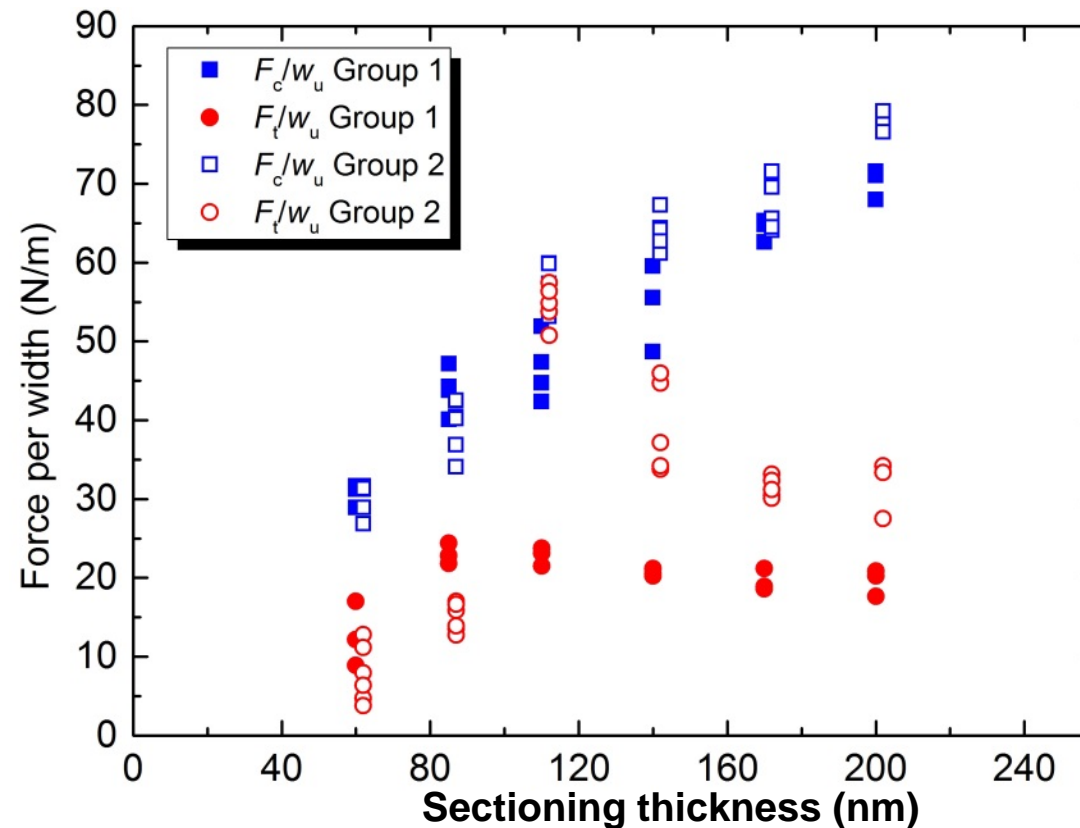
$$\frac{F_c}{w} = \left(\frac{\tau_y \gamma}{Q} \right) t_u + \frac{R}{Q}$$



Estimated division of dissipation mechanisms



Fracture toughness & Yield stress



Fracture energy R : ~10 J/m²

Shear yield stress τ_y : ~110 MPa

G_c =500-1000 J/m² at macroscopic

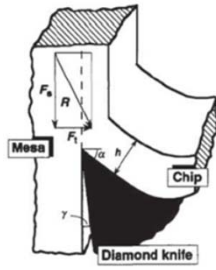
Close to *Patel et al.* (2009)

Scaling effect in polymer fracture



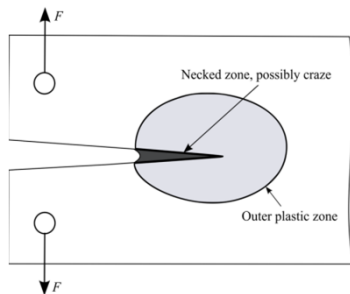
Intrinsic fracture energy
Breaking covalent bonds

1 J/m^2



Nanocutting
Fracture energy

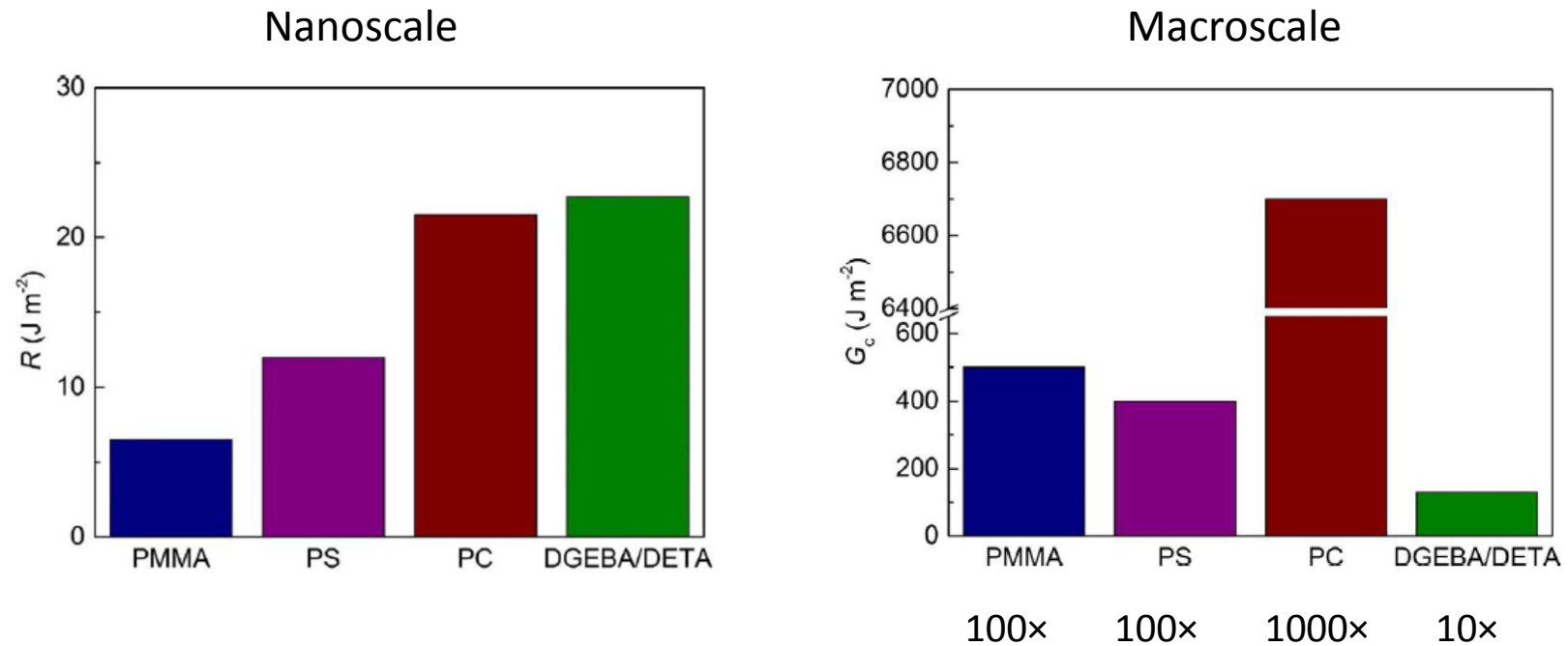
10 J/m^2



Macroscopic fracture toughness
Critical energy release rate

1000 J/m^2

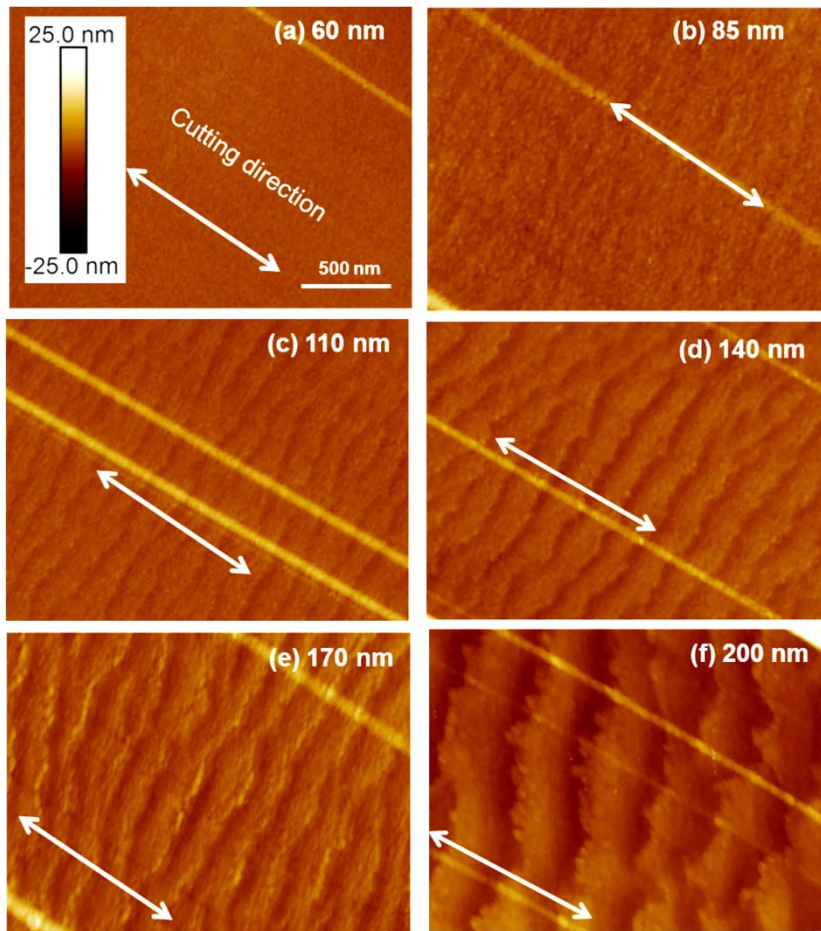
Nano-macro scale difference



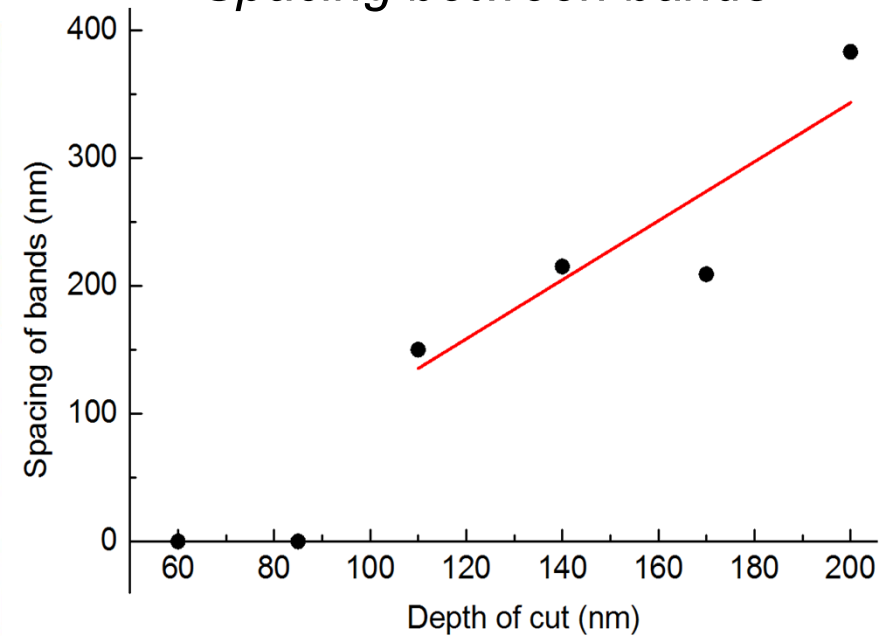
(Sun et al., 2017; Ericson & Lindberg, 1996, 1997; Kausch, 1987)

Characteristics of sectioned surfaces

AFM Morphologies, $v_0 = 1.0$ mm/s

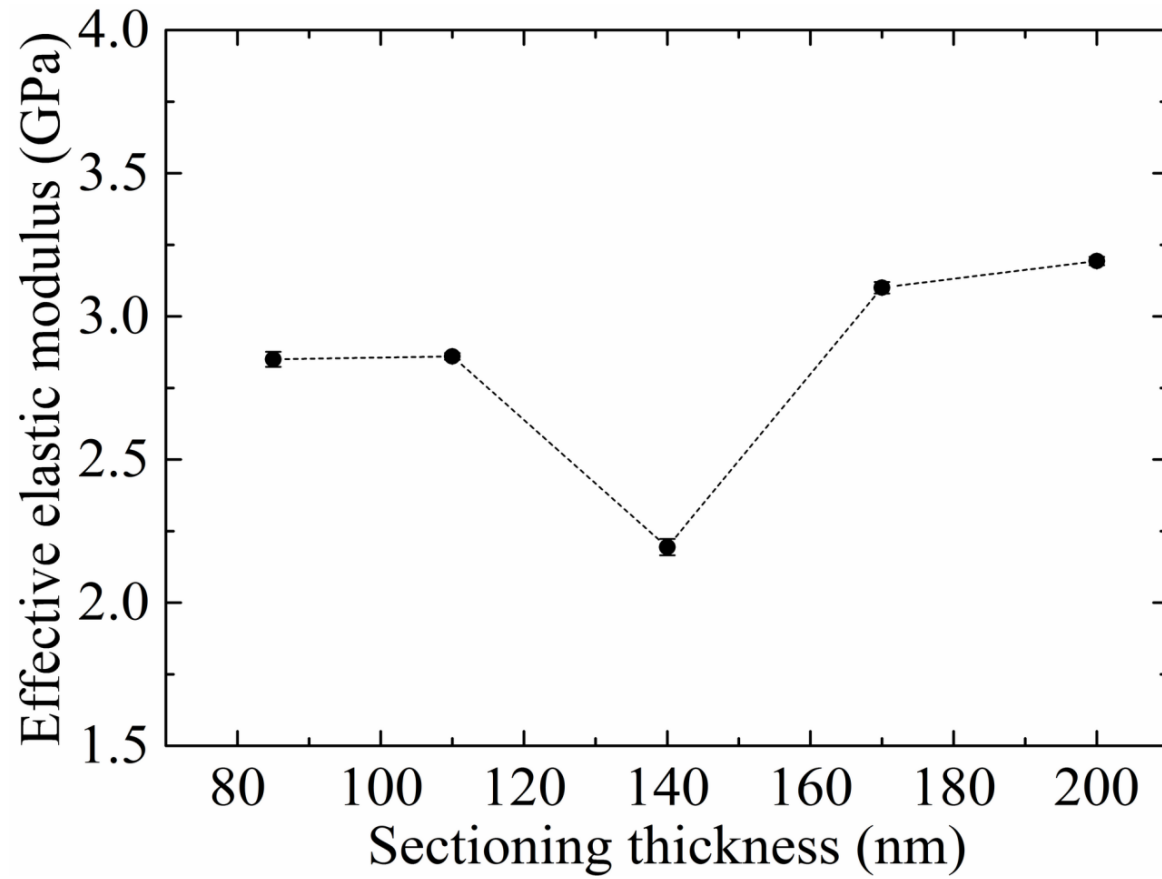


Spacing between bands



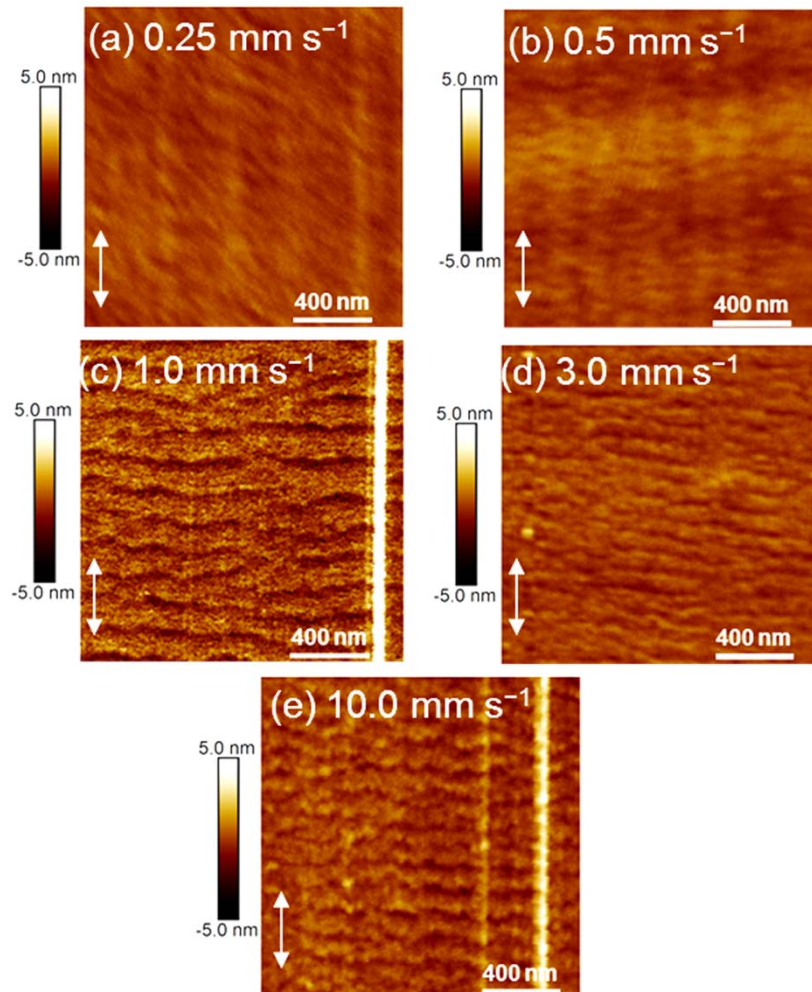
60 nm: flat and smooth
85 nm: feeble structures
110-200 nm: periodicity

Surface stiffness

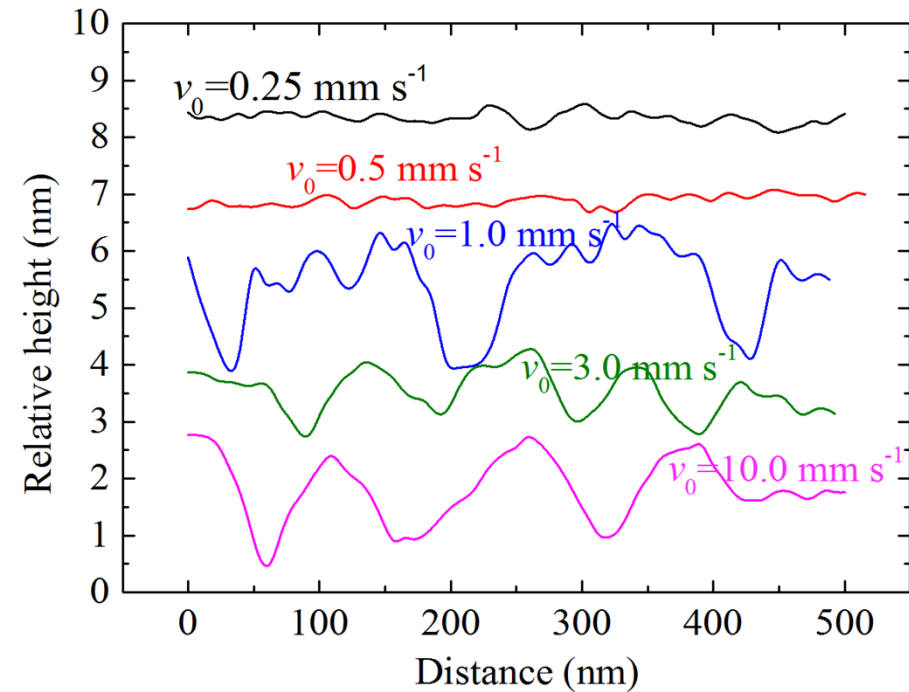


Characteristics of sectioned surfaces

AFM Morphologies, $t_u=85$ nm

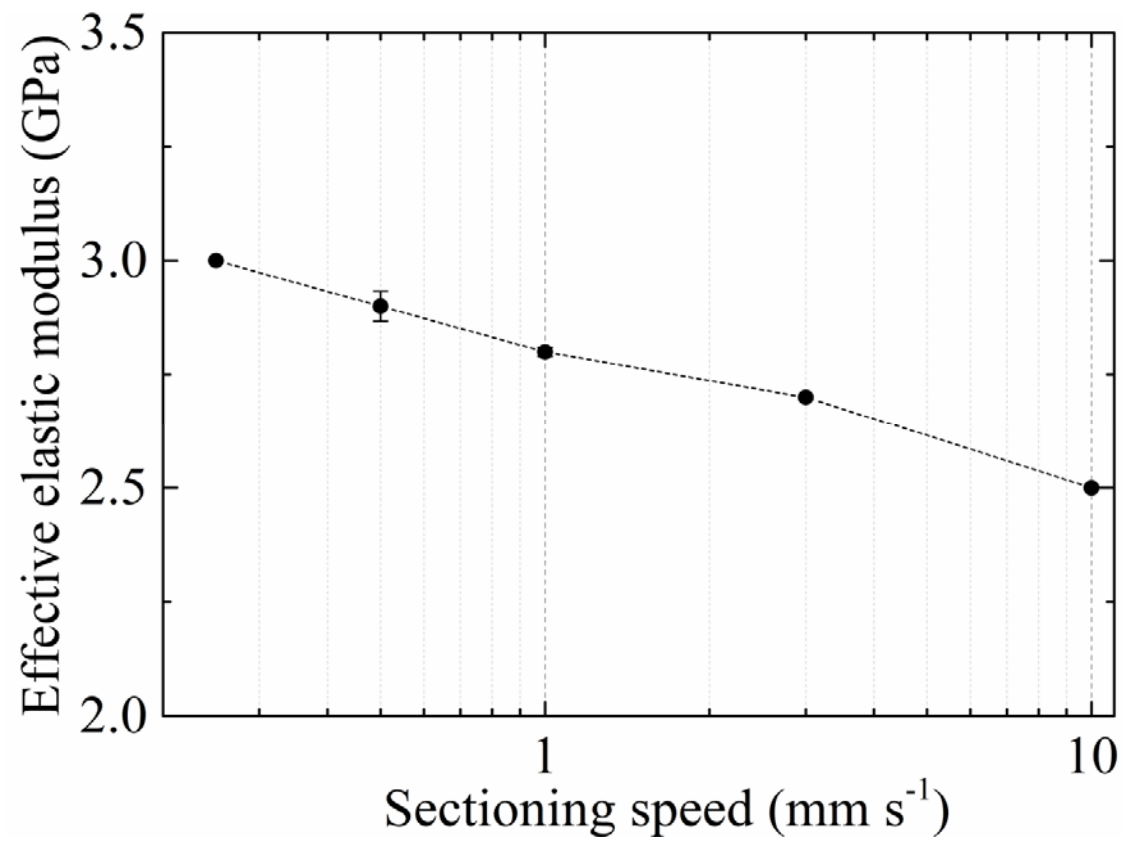


Height along sectioning



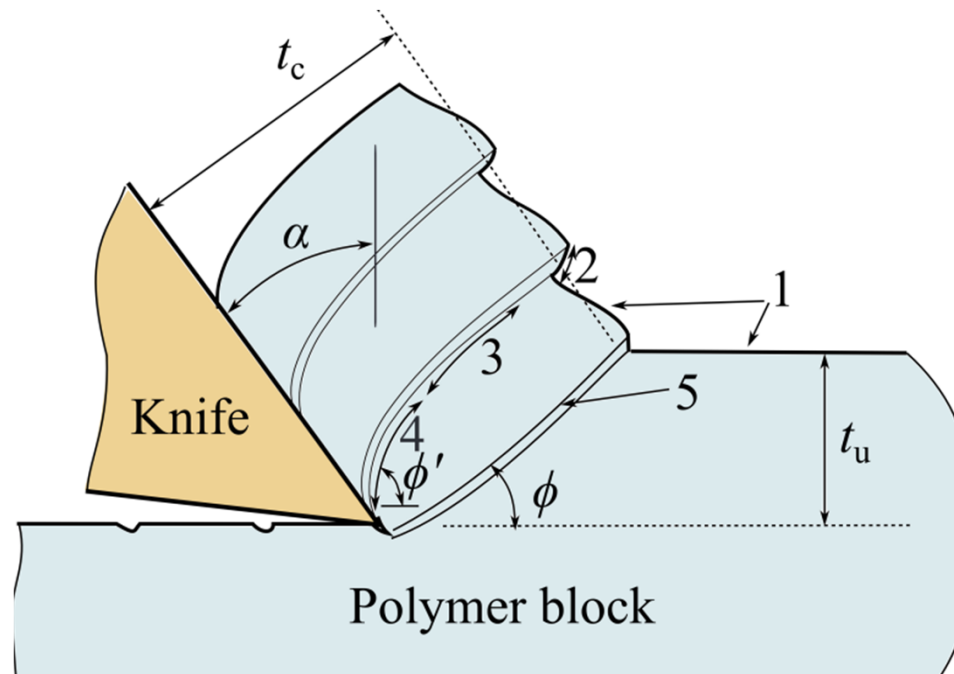
0.25, 0.5 mm/s: flat surfaces
1.0-10.0 mm/s: periodicity

Surface stiffness



Hypothesis: shear banding

Critical sectioning conditions for the onset of periodic structures, a typical feature of shear banding in sectioning



Heat generation



Heat localisation



Thermal softening

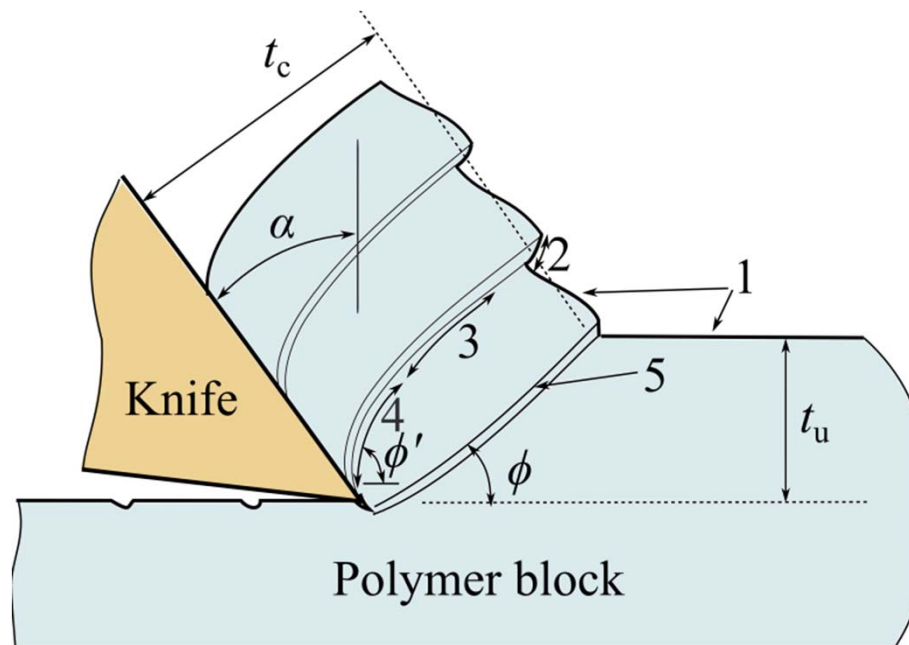


Shear band

(After Komanduri & Hou, 2002; Turley et al. 1982)

Several contributing heat sources affect shear yielding

Critical cutting conditions exist to form periodic structures on the surfaces, a typical feature of shear banding in cutting

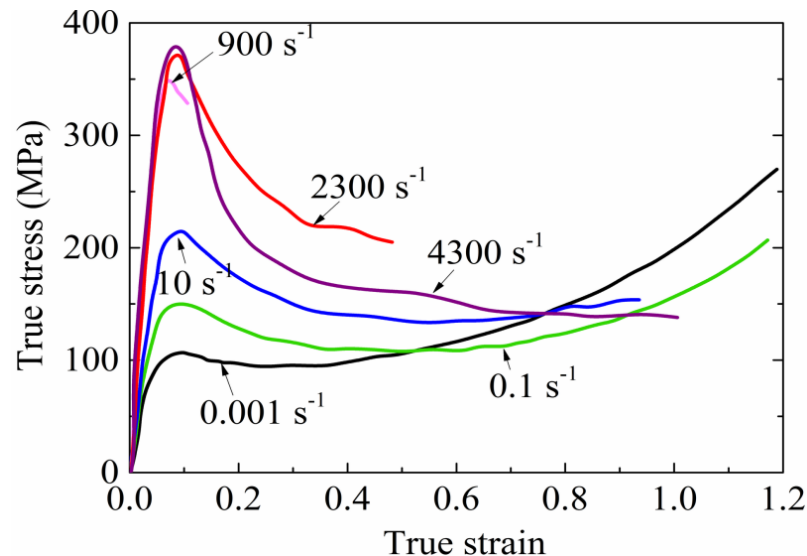


1. undeformed surfaces
2. yielded surface due to localised shear,
3. shear band
4. shear band segment near knife edge
5. localised deformation in the shear plane emanating from the knife tip.

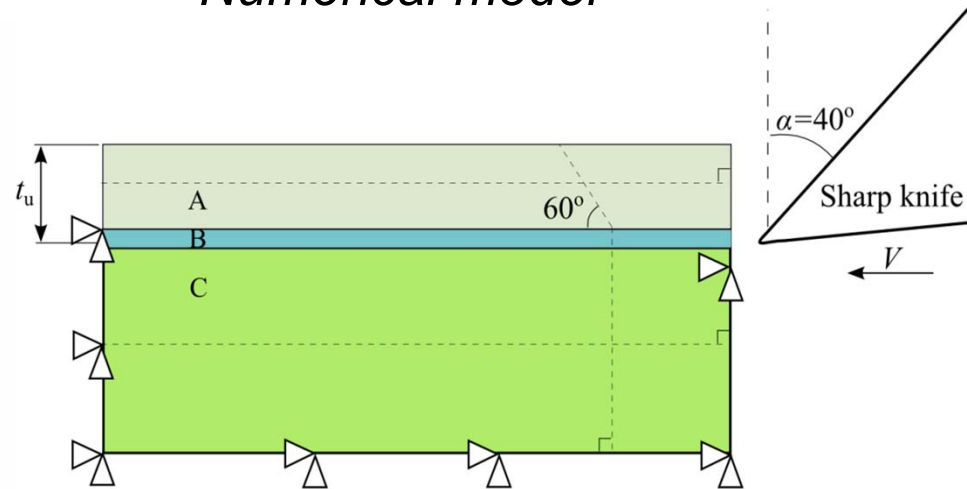
Schematic of the shear banding during cutting.
(after Komanduri & Hou, 2002; Turley *et al.* 1982)

FE modelling

σ - ϵ for PMMA, Richeton (2005)



Numerical model



Abaqus/Explicit

Thickness: 85 nm, speed: 1.0 mm/s

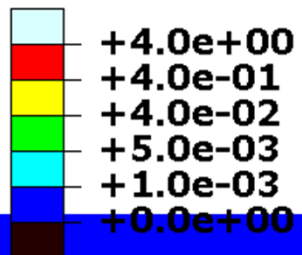
Yield & post-yield of PMMA: *Richeton* (2005) in A, B, C

Fracture model: strain based failure criterion in B

FE modelling

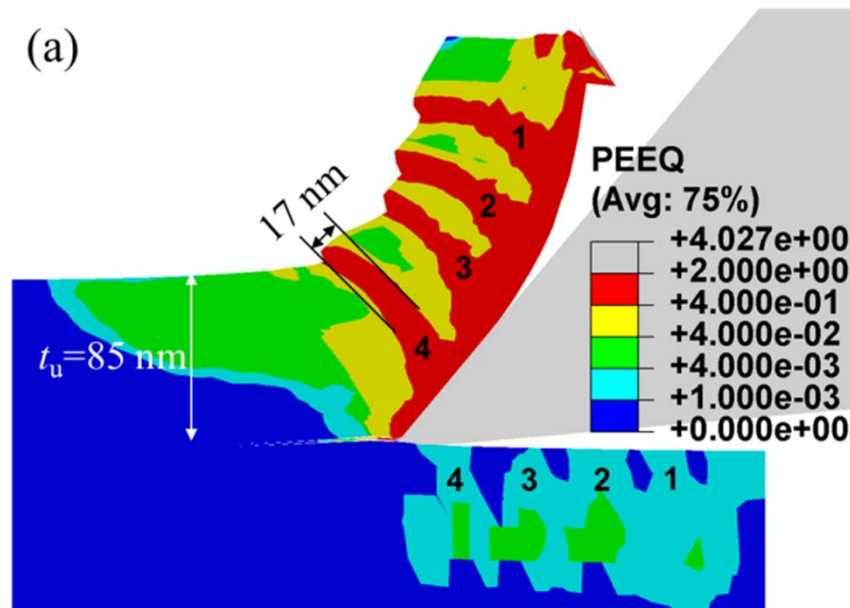
Step: Step-1 Frame: 0
Total Time: 0.000000

PEEQ
(Avg: 75%)

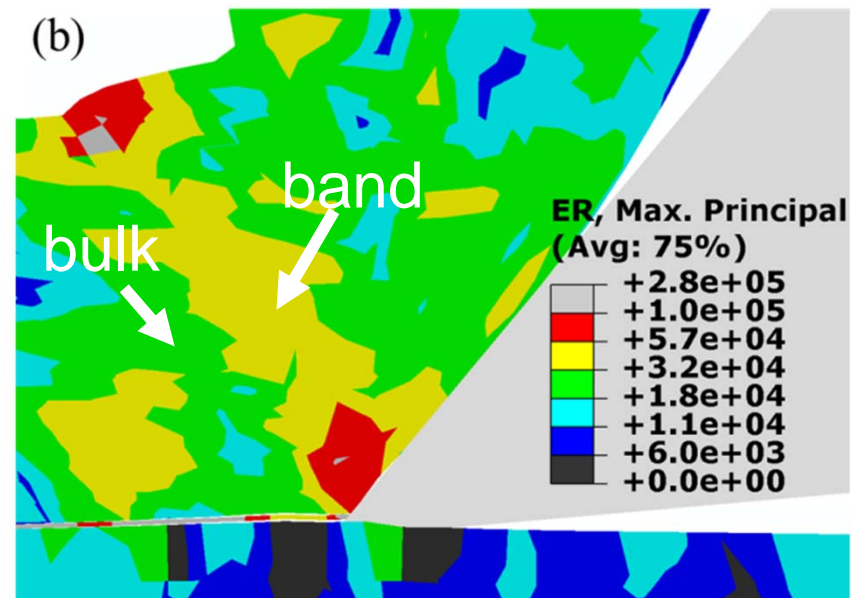


FE modelling

Equivalent plastic strain



Maximum principle strain rate (/s)

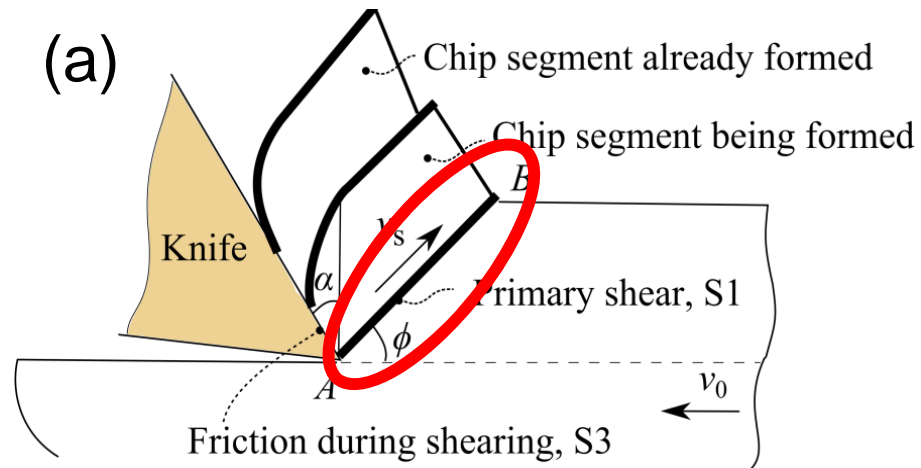


Band width = $1/5$ of sectioning thickness

Strain rate in bulk = $1/3-1/2$ of the rate in the band

(consistent with *Özel, 2006; Childs, 2013*)

Adiabatic shear modelling



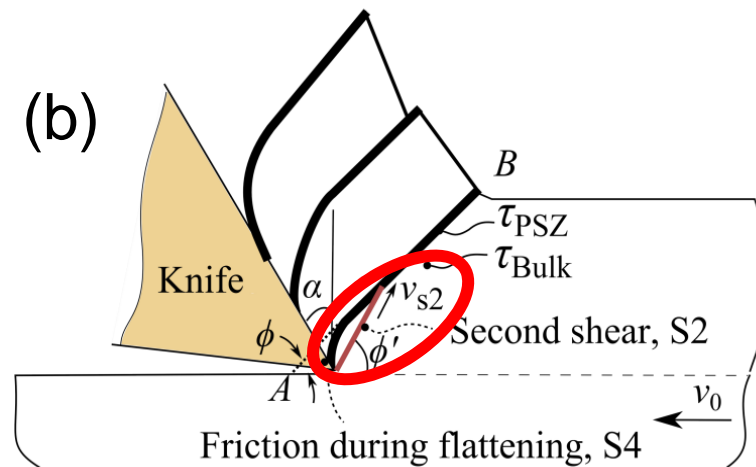
Onset criterion : $\tau_{\text{PSZ}} \leq \tau_{\text{Bulk}}$

Constitutive law for PMMA:

$$\tau_{\text{PSZ}} \ \& \ \tau_{\text{Bulk}} = f(T, \dot{\gamma})$$

$$\sigma_y = \sigma_i(0) - mT + \frac{2k_B T}{V_a} \sinh^{-1} \left(\frac{\dot{\epsilon}}{\dot{\epsilon}_0 \exp(-\Delta H_\beta / k_B T)} \right)^{1/n}$$

Richeton et al. (2005)



Strain rate:

$$\dot{\gamma}_{\text{PSZ}} = \frac{v_s}{\Delta h} \quad (\text{from FEA})$$

$$\dot{\gamma}_{\text{Bulk}} = \dot{\gamma}_{\text{PSZ}} / 3$$

*Adiabatic shearing model by
Komanduri & Hou (2002)*

Adiabatic shear modelling

Temperature in primary shear zone:

Heat S1-S4 + Preheating due to S1-S4

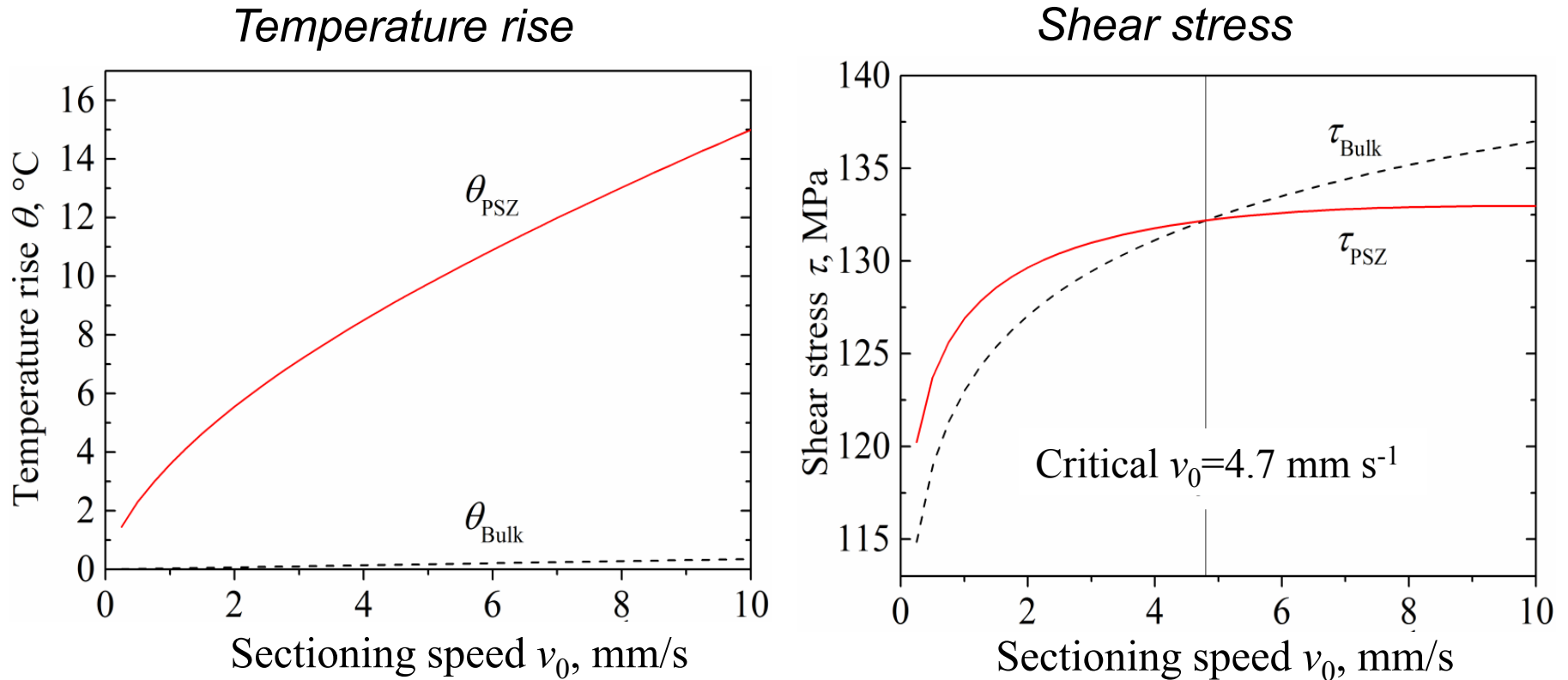
e.g. Heat S1

$$\theta_M = \frac{q_1}{2\pi\lambda} \left(1 - \frac{t}{2t_0}\right) \int_0^{l_s} \Omega(p) dy_i + \frac{q_0}{16\pi\lambda\alpha_t t_0} \int_0^{l_s} r_i^2 \chi(p) dy_i$$

Temperature in bulk:

Preheating due to S1-S4

Adiabatic shear modelling

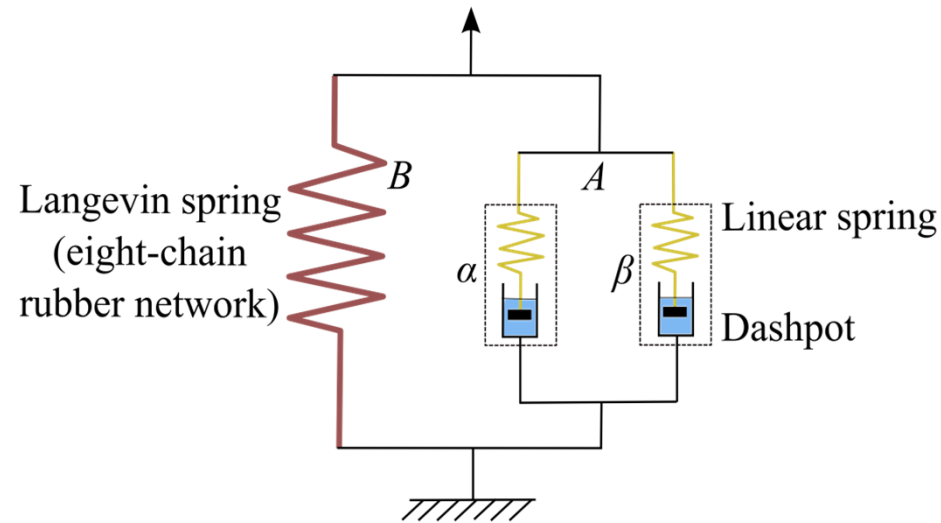


The estimated speed for the onset of shear bands agrees with the experiment

FE modelling of PMMA sectioning

Elastic viscoplastic model

Mulliken-Boyce model



Total stress :

$$\mathbf{T} = \mathbf{T}_\alpha + \mathbf{T}_\beta + \mathbf{T}_B$$

Cauchy stresses in α and β

$$\mathbf{T}_\alpha = \frac{1}{J_\alpha} \mathbf{L}_\alpha^e [\ln \mathbf{V}_\alpha^e], \quad \mathbf{T}_\beta = \dots$$

Back stress in B

$$\mathbf{T}_B = \frac{C_R}{3} \frac{\sqrt{N}}{\lambda_{\text{chain}}^p} \mathbf{L}^{-1} \left(\frac{\lambda_{\text{chain}}^p}{\sqrt{N}} \right) \bar{\mathbf{B}}'_B$$

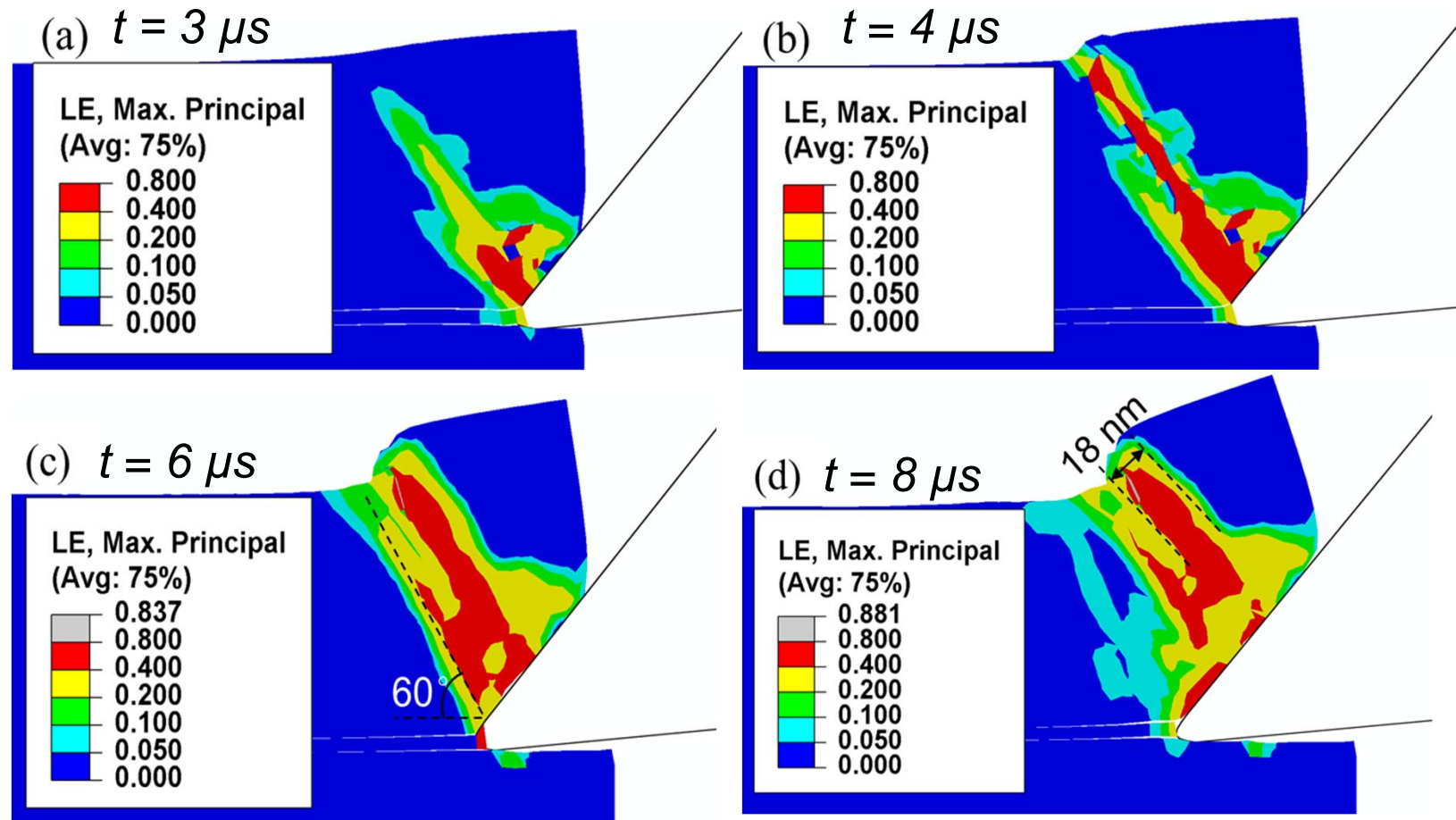
Plastic flow in α and β

$$\dot{\gamma}_\alpha^p = \dot{\gamma}_{0,\alpha}^p \exp \left[-\frac{\Delta G_\alpha}{k\theta} \left(1 - \frac{\tau_\alpha}{t_\alpha \hat{s}_\alpha + \alpha_{p,\alpha} p} \right) \right], \quad \dot{\gamma}_\beta^p = \dots$$

Adiabatic heating

$$\dot{\theta} = \frac{1}{\rho c} \left[\text{tr}(\mathbf{T}_\alpha \tilde{\mathbf{D}}_\alpha^p) + \text{tr}(\mathbf{T}_\beta \tilde{\mathbf{D}}_\beta^p) \right]$$

FEA results



Periodic structures are reproduced

Recapitulation so far

- The fracture energy of PMMA is as low as ~ 10 J/m² by nanosectioning test
- Critical sectioning conditions (sectioning thickness, speed) are identified for the onset of periodic structures
- The periodic structures are attributed to localised shear deformation
- The adiabatic shear model and elastic viscoplastic model could be used to predict shear banding during sectioning

Macroscale:

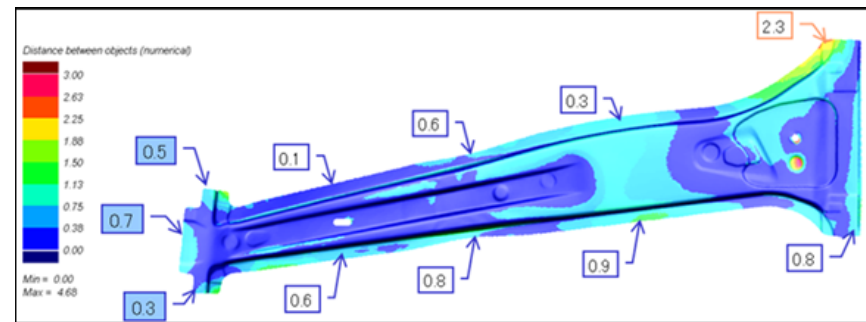
Materials modelling and mechanical characterization in metal forming

Sheet metals forming
Stamping



(Atlas Tool Inc.)

Finite element modelling
Including plasticity



(ESI Group)

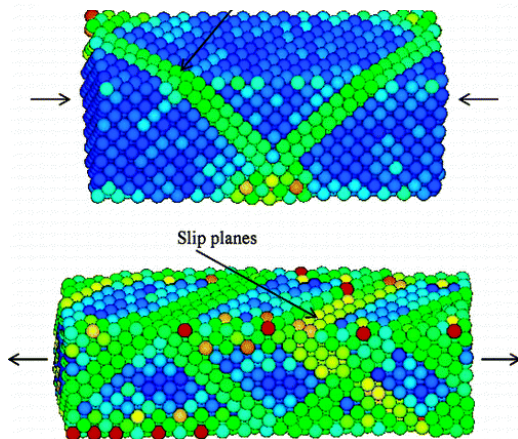
Modeling has unlocked breakthroughs in macroscale manufacturing

Nanoscale:

Materials modelling and mechanical characterization at sub-micron scale

Metals

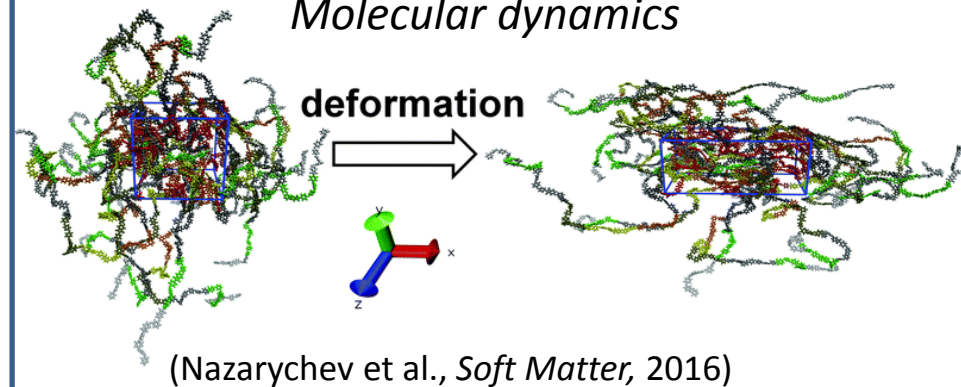
Atomistic simulations



(Diao et al., *Nano Letters*, 2004)

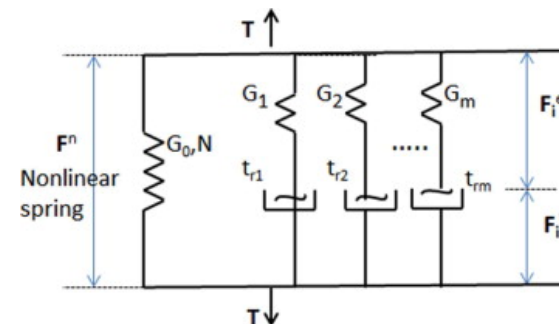
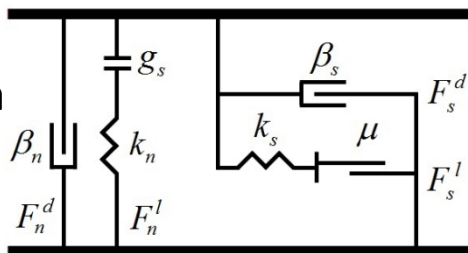
Polymers

Molecular dynamics

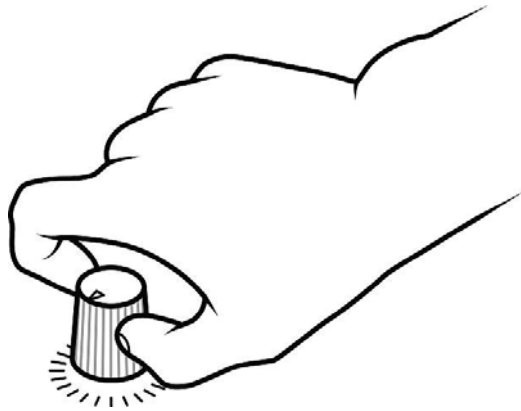


(Nazarychev et al., *Soft Matter*, 2016)





Continuum models



Model-based control of manufacturing parameters



Turning the knobs sensibly...

-  Feeding rate [$\mu\text{m/s}$]
-  Rotational speed [rpm]
-  Cutting depth [nm]
-  Temperature [$^{\circ}\text{C}$]

Smooth



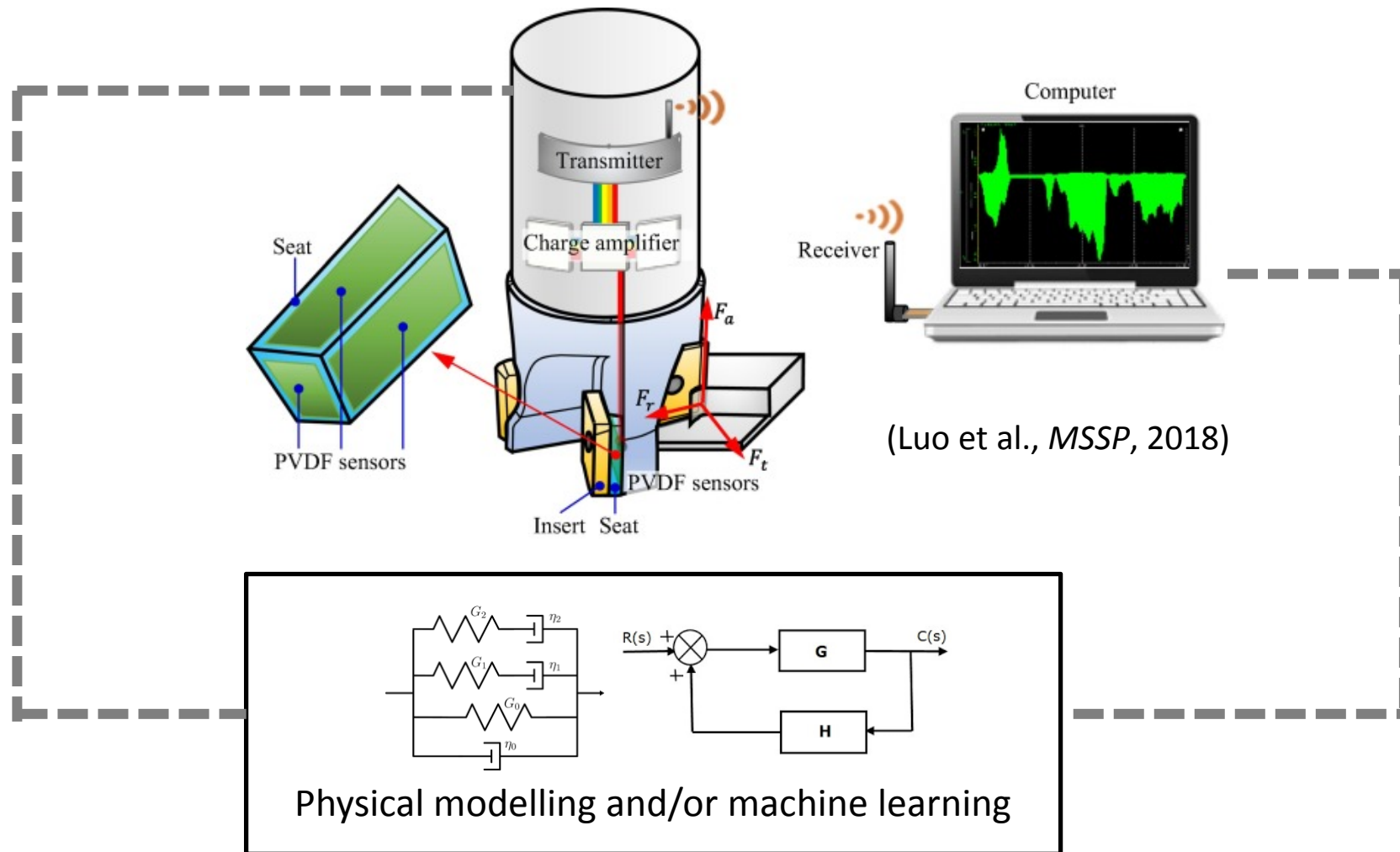
or

Rough



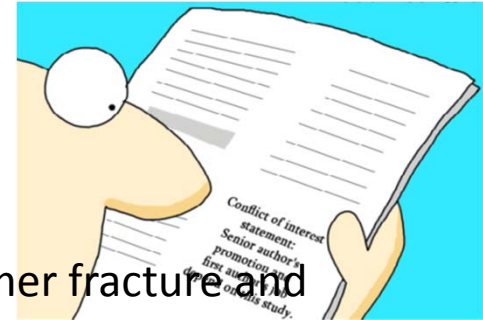
Future prospects:

On-line monitoring of tool forces...



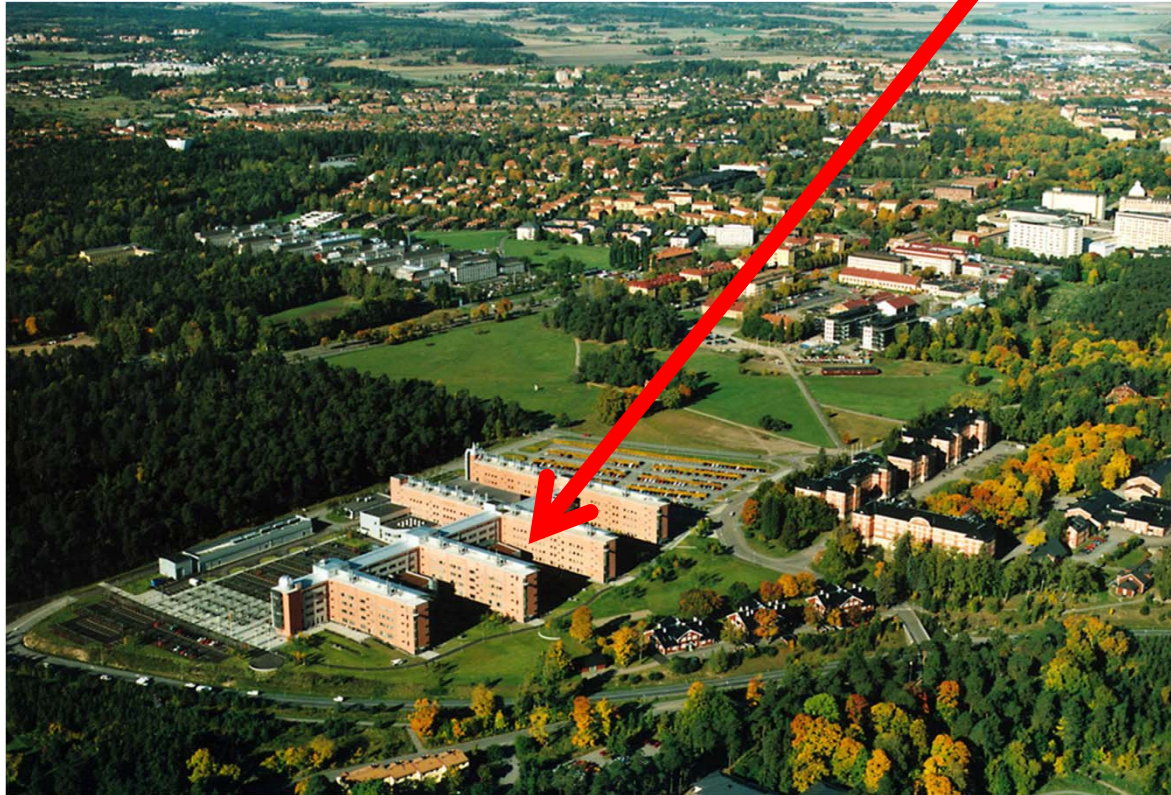
... with feedback for optimal control

Related publications:



- Sun, F., Li, H., Lindberg, H., Leifer, K. and Gamstedt, E.K., “Polymer fracture and deformation during nanosectioning in an ultramicrotome”, *Engineering Fracture Mechanics*, **182** (2017), 595-606. DOI: 10.1016/j.engfracmech.2017.05.044
- Sun, F., Li, H., Leifer, K. and Gamstedt, E.K., “Rate effects on localized shear instabilities in nanosectioning of an amorphous thermoplastic polymer”, *International Journal of Solids and Structures*, **129** (2017), 40-48. DOI: 10.1016/j.ijsolstr.2017.09.016
- Sun, F., Li, H., Leifer, K. and Gamstedt, E.K., “Effect of nanosectioning on surface features and stiffness of an amorphous glassy polymer”, *Polymer Engineering and Science*, available on-line, 2018. DOI: 10.1002/pen.24793
- Sun, F., Wiklund, U., Avilés, F. and Gamstedt, E.K., “Assessing local yield stress and fracture toughness of carbon nanotube poly(methyl methacrylate) composite by nanosectioning”, *Composites Science and Technology*, **153** (2017), 95-102. DOI: 10.1016/j.compscitech.2017.09.034
- Sun, F. and Gamstedt, E.K., “Experimental and numerical investigation on shear banding during nanomachining of an amorphous glassy polymer”, submitted to *International Journal of Mechanical Sciences*, 2018.

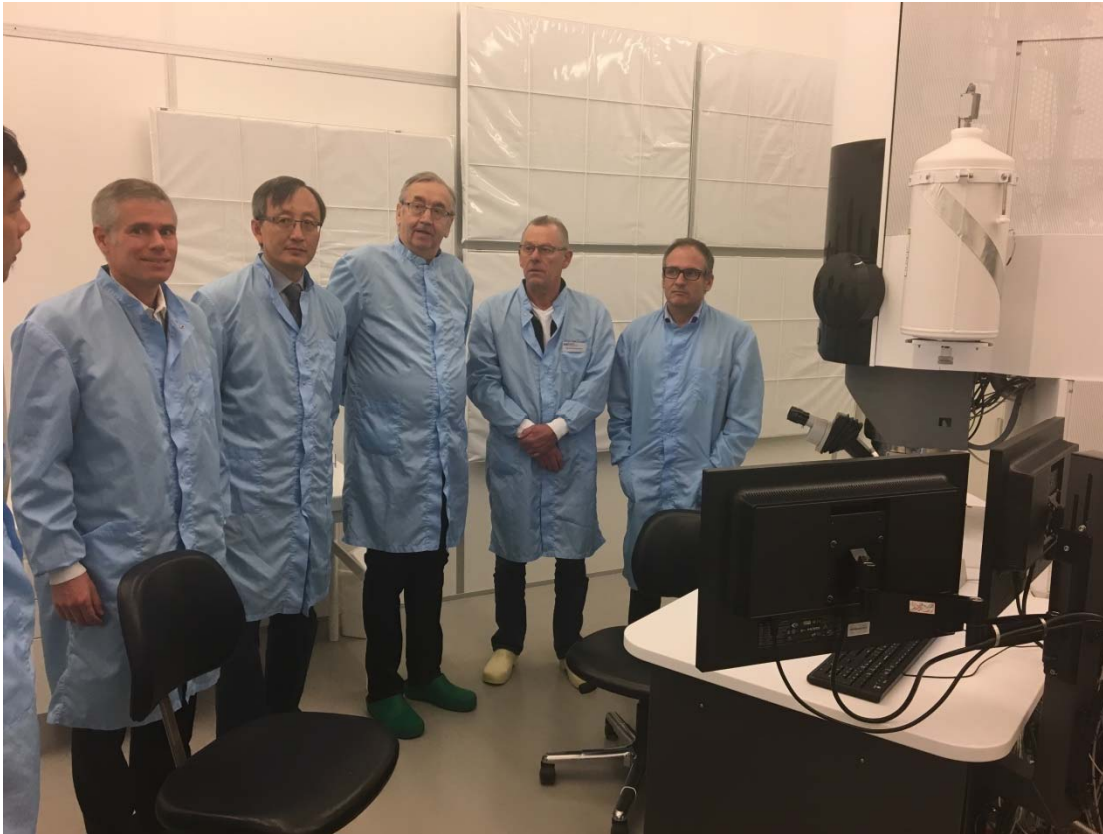
Welcome to the Ångström Laboratory at Uppsala University!



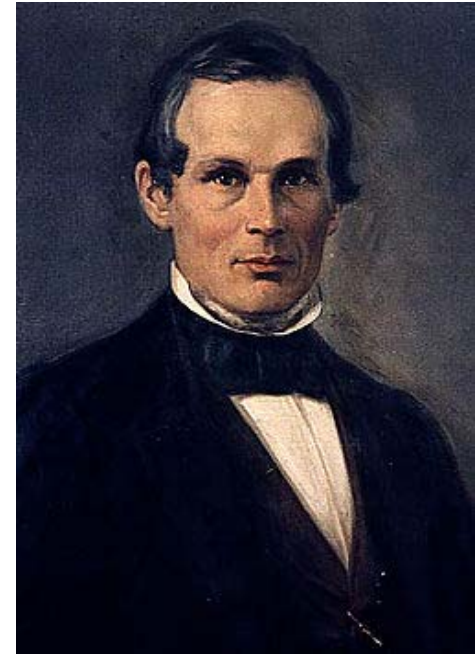
Ångström Laboratory: House 4, floor 2

<http://www.teknik.uu.se/applmech>

Particular thanks to Kai Cheng and his team!



Visiting the Ångström Laboratory in Uppsala (2017)



Anders Ångström
Uppsala University



FIFA WORLD CUP
RUSSIA 2018

QARTER - FINALS

SWEDEN V ENGLAND

SAMARA ARENA SATURDAY 7TH JULY 2018 - 16:00

DESIGN BY : JAFAR
WWW.JEFFWALLPAPERS.COM

adidas Coca-Cola 万达 WANDA Sberbank HYUNDAI QATAR AIRWAYS VISA

Questions or comments?

